Weather Forecasting then: Weather rules, have a look to the west ... Weather Forecasting today: Use of super-computers.

Idea of Numerical Weather Prediction (NWP): L.F.Richardson 1921

Dynamics of the atmosphere can be described by six parameters.

6 Parameters: Temperature, pressure, humidity, wind (u,v,w)

6 Equations: Newton: Force = mass * acceleration

Laws of thermodynamics

Conservation of mass (continuity equation)

Hydrostatic equation

This system of equations can be solved! Experiment with students...

Primitive Equations to compute global atmospheric flow

Three main sets of Balance Equations

- 1. Continuity Equation
 Representing the Conservation of Mass
- 2. Conservation of momentum (Navier-Stokes-Equations)
 Describing the atmospheric flow over the surface
- 3. Thermal Energy Equation

 Describing the Temperature of the System with sinks and sources

Primitive Equations to compute global atmospheric flow

- 1. Pressure Gradient Force: Force = mass * acceleration (Newton)
- 2. Navier-Stokes-Equations describing friction near surface
- 3. Equation of motion for 3 components x,y,z
- 4. Continuity Equation describing conservation of mass
- 5. Thermal Energy Equations to comply with the Laws of Thermodynamics

With a given initial state (numerical analysis of observations) this set of equations describes the rate of change of the system so that numerical integration allow to compute the system in the future, Weather Forecast.

Forces that cause atmospheric motion

Forces that cause atmospheric motion include the pressure gradient force, gravity, and viscous friction. Together, they create the forces that accelerate our atmosphere.

The pressure gradient force causes an acceleration forcing air from regions of high pressure to regions of low pressure. Mathematically, this can be written as:

$$\frac{f}{m} = \frac{1}{\rho} \frac{dp}{dx}$$

The gravitational force accelerates objects at approximately 9.8 m/s² directly towards the center of the Earth.

The force due to viscous friction can be approximated as:

$$f_r = rac{f}{a} rac{1}{
ho} \mu \left(
abla \cdot (\mu
abla v) +
abla (\lambda
abla \cdot v)
ight).$$

Using Newton's second law, these forces (referenced in the equations above as the accelerations due to these forces) may be summed to produce an equation of motion that describes this system. This equation can be written in the form:

$$egin{aligned} rac{dv}{dt} &= -(1/
ho)
abla p - g(r/r) + f_r \ g &= g_e \,. \end{aligned}$$

Therefore, to complete the system of equations and obtain 6 equations and 6 variables:

$$\begin{split} & \bullet \frac{dv}{dt} = -(1/\rho)\nabla p - g(r/r) + (1/\rho)\left[\nabla \cdot (\mu \nabla v) + \nabla (\lambda \nabla \cdot v)\right] \\ & \bullet c_v \frac{dT}{dt} + p \frac{d\alpha}{dt} = q + f \\ & \bullet \frac{d\rho}{dt} + \rho \nabla \cdot v = 0 \\ & \bullet p = nT. \end{split}$$

where n is the number density in mol, and T:=RT is the temperature equivalent value in Joule/mol.

Courant – Friedrich – Lewy Condition (CFL)

The Courant–Friedrichs–Lewy or CFL condition is a condition for numerical stability

The distance that any information travels during the timestep length within the mesh must be lower than the distance between mesh elements.

In other words, information from a given cell or mesh element must propagate only to its immediate neighbors.

$$C = a \frac{\Delta t}{\Delta x}$$

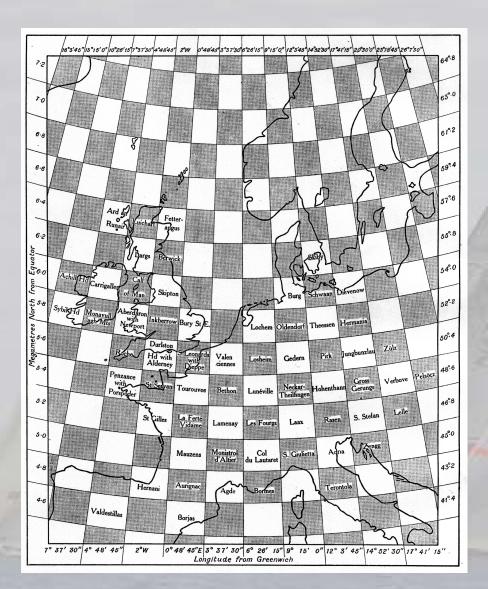
 $C = a \frac{\Delta t}{\Delta x}$ α = characteristic speed so that C = C courant number becomes dimensionless

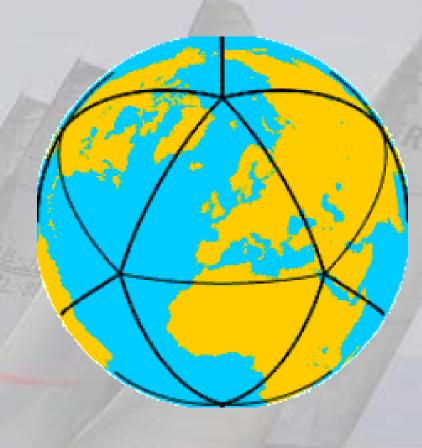
C ≤ 1 is necessary for numerical stability

If C > 1, the numerical viscosity would be negative (!?)

NUMERICAL WEATHER PREDICTION - THEN AND NOW

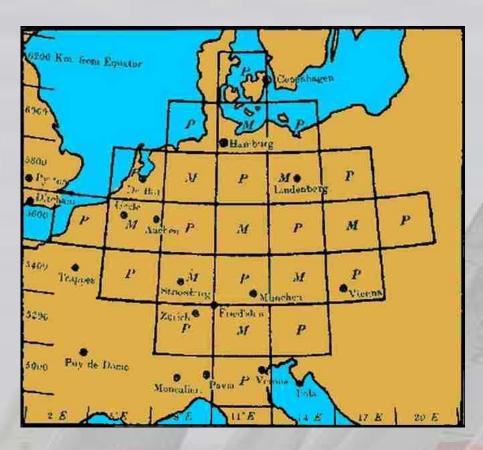
L.F.Richardson 1921 Deutscher Wetterdienst 2021

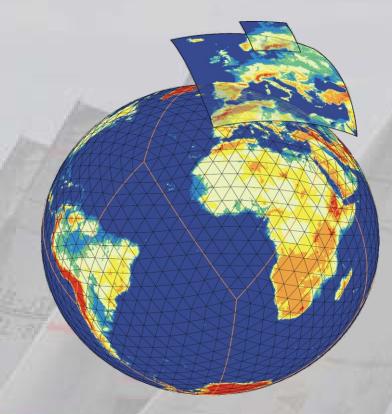




NUMERICAL WEATHER PREDICTION - THEN AND NOW

L.F.Richardson 1921 Deutscher Wetterdienst 2021





Problem:

1921: runtime > realtime ...

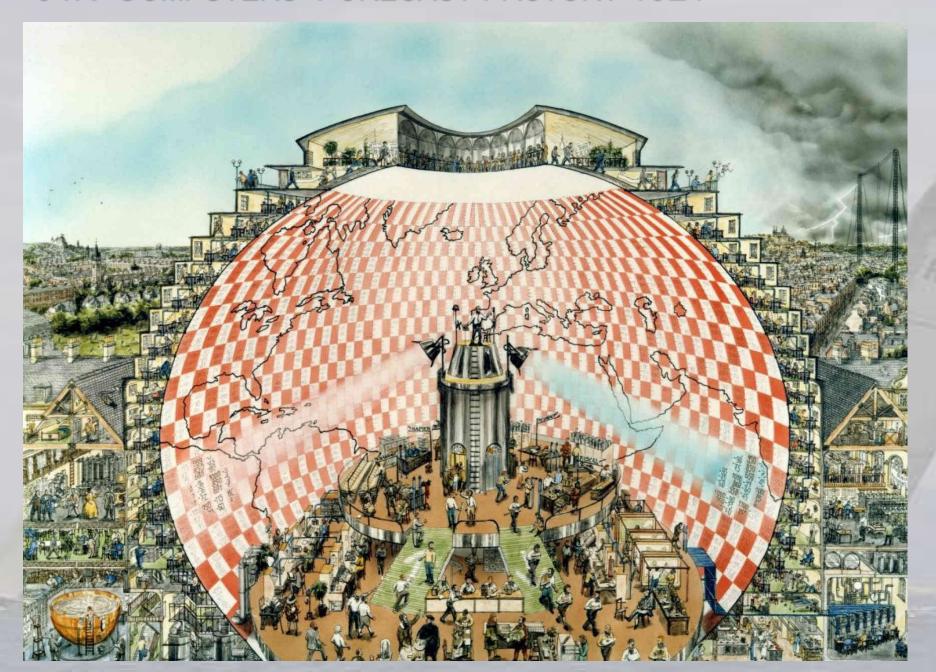
2018: H + 24: 20 minutes

H +174: 2 hours

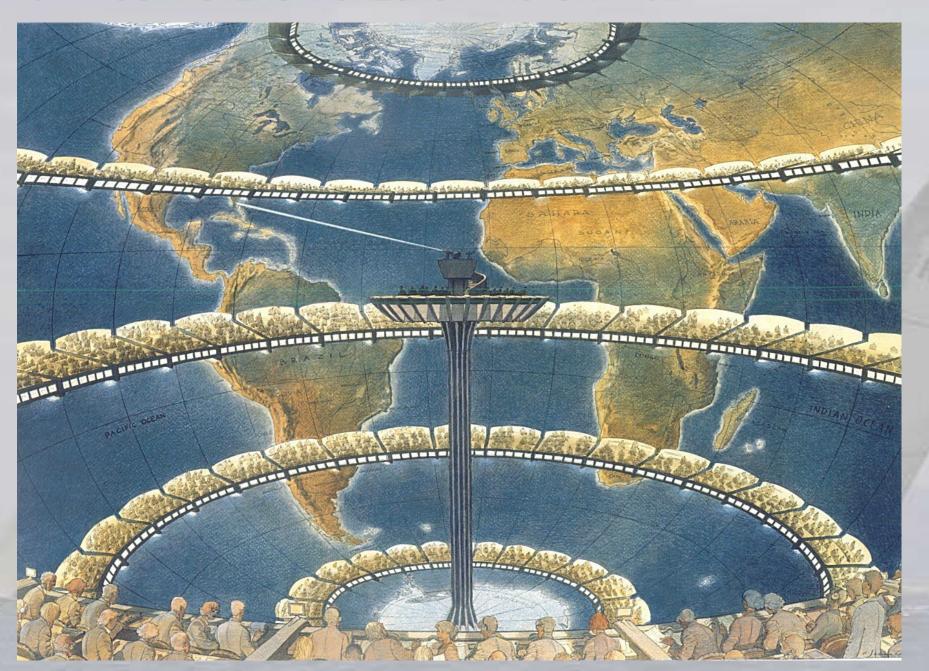
Model Resolution / km Layers Gridpoints/ Mio 265 /

ICON / EU / DE 13 / 6.5 / 2.2 90/

64K 'COMPUTERS' FORECAST FACTORY 1921



64K 'COMPUTERS' FORECAST FACTORY 1921

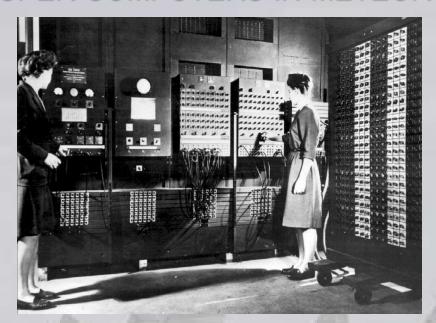


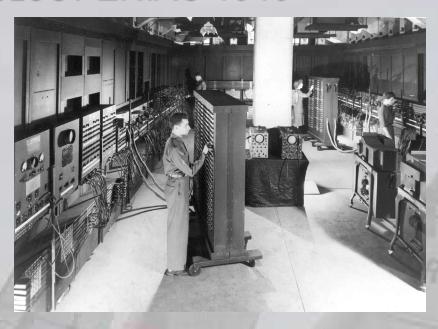
64K 'COMPUTERS' FORECAST FACTORY 1921

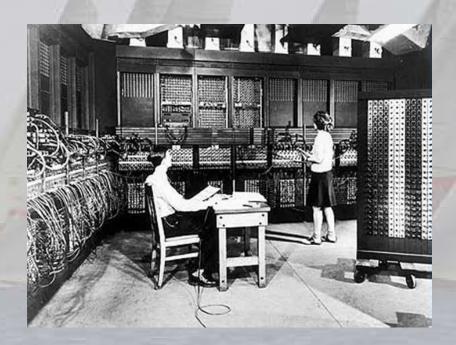


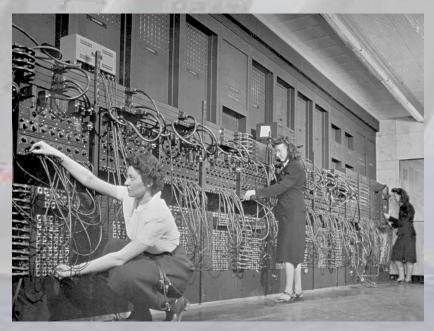
"64,000 computers would be needed to race the weather for the whole globe..." A cartoon showing Richardson's vision of a central forecasting factory. (L.S. Gandin (1965) 'Machines forecast the weather', Gidrometeoizdat, Leningrad)

SUPER COMPUTERS IN METEOROLOGY ENIAC 1946









Publications for Use of Supercomputers in NWP

S V E N S K A G E O F Y S I S K A F Ö R E N I N G E N

VOLUME 2, NUMBER 4 Tellus NOVEMBER 1950

A QUARTERLY JOURNAL OF GEOPHYSICS

Numerical Integration of the Barotropic Vorticity Equation

By J. G. CHARNEY, R. FJÖRTOFT¹, J. von NEUMANN The Institute for Advanced Study, Princeton, New Jersey²

(Manuscript received 1 November 1950)

PUBLICATIONS FOR USE OF SUPERCOMPUTERS IN NWP

Numerical Integration of the Barotropic Vorticity Equation

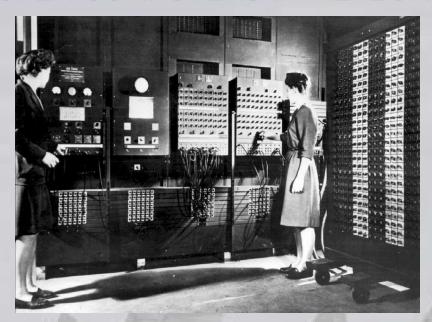
By J. G. CHARNEY, R. FJÖRTOFT¹, J. von NEUMANN The Institute for Advanced Study, Princeton, New Jersey²

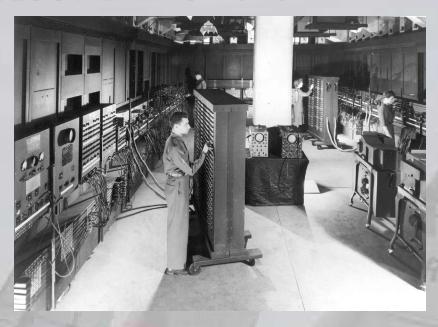
(Manuscript received 1 November 1950)

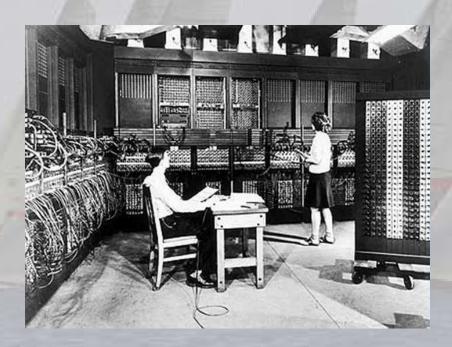
Abstract

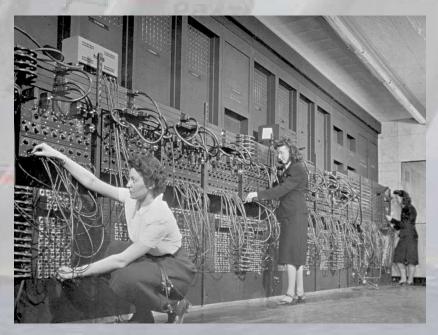
A method is given for the numerical solution of the barotropic vorticity equation over a limited area of the earth's surface. The lack of a natural boundary calls for an investigation of the appropriate boundary conditions. These are determined by a heuristic argument and are shown to be sufficient in a special case. Approximate conditions necessary to insure the mathematical stability of the difference equation are derived. The results of a series of four 24-hour forecasts computed from actual data at the 500 mb level are presented, together with an interpretation and analysis. An attempt is made to determine the causes of the forecast errors. These are ascribed partly to the use of too large a space increment and partly to the effects of baroclinicity. The rôle of the latter is investigated in some detail by means of a simple baroclinic model.

SUPER COMPUTERS IN METEOROLOGY ENIAC 1946









SUPER COMPUTERS IN METEOROLOGY TODAY



DWD NEC SX-9 2008 - 2014



UK Metoffice Cray XC-40



DWD Cray XC-40 2013 - today



European Center ECMWF Cray XC-40

AIRCRAFT 1927 – 1969 – 2007 – TODAY TECHNOLOGICAL PROGRESS – ASYMPTOTICALLY TOWARDS OPTIMUM



1927 Spirit of St.Louis



Lufthansa Lufthansa

1969 Boeing B747-100 Concorde



2007 Boeing 747-400 Airbus A380

Today Airbus A350, Boeing 777

COMPUTATION TIME FOR A 3-DAY-FORECAST ...

A 3-day-forecast requires approx. 1 Trillion (1 000 000 000 000 000 = 10^{15}) floating-point-operations (FLOP) which can be achieved as follows:

		Computer po	ower runtime	increase
Pocket computer	ca. 1	FLOP/s	32 Mio. years	
ENIAC 1946 USA	ca. 5	10^3 KIL	O 6.000 years	
Laptop	ca. 1	10^9 GIG	GA 12 days	* 200.000
Supermarket PC	ca. 3.5	10^9 GIG	GA 3 days	* 3.5
DWD HPC Cray XC40	ca. 50	10^12 TE	RA < 1 hour	* 15.000
TOP-500 #1 2020 CHINA	ca. 100	10^15 PE	TA < 1 minute	* 20
TOP-500 #1 2022 USA	ca. 1	10^18 EX	A	

2022 TOP-500 SUPER COMPUTERS #1 FRONTIER USA EXA-FLOPS

Rank 1

TOP500

NOV 2022

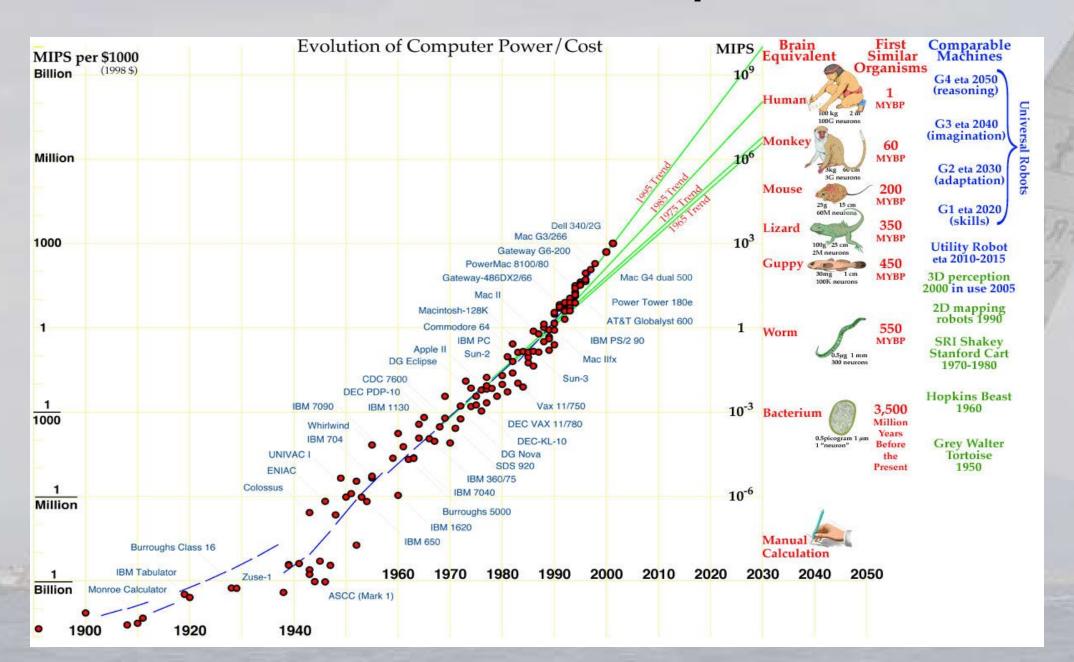
System
Frontier - HPE
Cray EX235a,
AMD Optimized

3rd Generation EPYC 64C 2GHz, AMD Instinct MI250X,

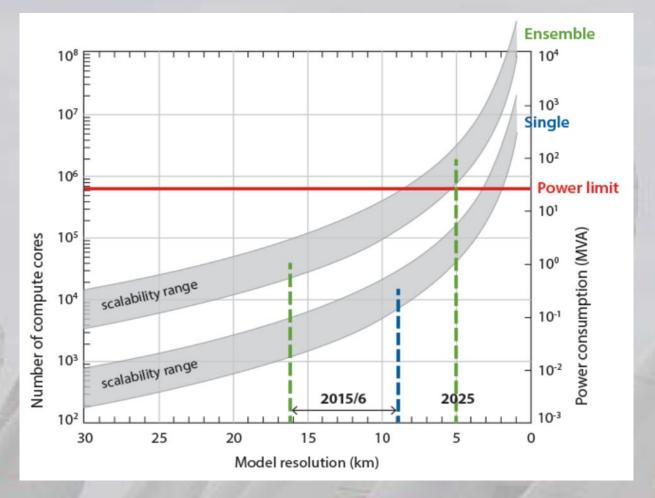
Slingshot 11,
HPE
DOE/SC/Oak
Ridge National
Laboratory
United States



Moore's Law of Growth of Computer Power



How will it go on? What can we expect from the computers in the future?



The goal is to increase the model resolution, which requires more powerful computers. These will be developed, but... They need more electrical power and the budget for power is limited. Currently it would allow a global model resolution of 3 km for single run and 7 km for ensemble run.

Requirement: Bring data into a formalized code to allow easier

- > Telecommunications
- Data processing
- Data compression

Code-Form Alphanumeric to comply with RTTY regulations, e.g. groups of 5-characters...

Today mostly binary for computerized decoding

Managed by WMO World Meteorological Organisation, Geneva

Used worldwide by all countries to allow global operations

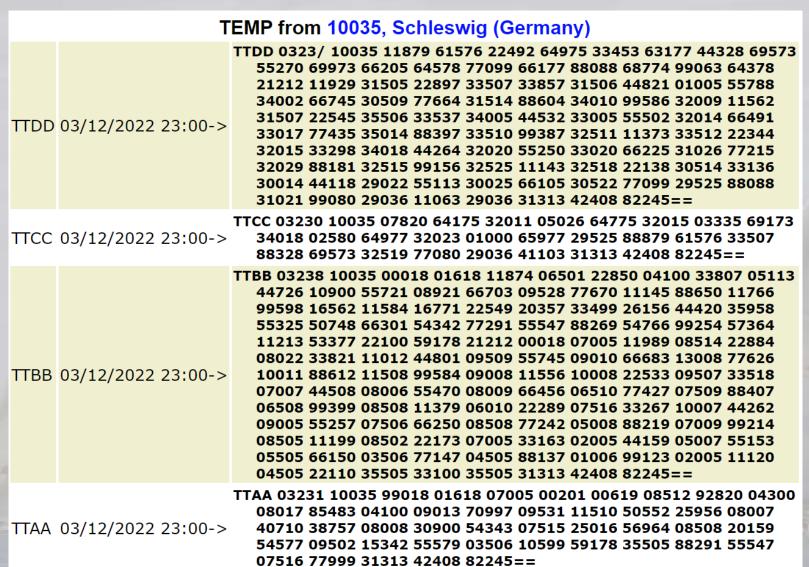
Codes for Surface Observations FM12 SYNOP Synoptic Surface Observation

```
# SYNOPS from 10091, Arkona (Germany) | 54-41N | 013-26E | 42 m
202212041800 AAXX 04181 10091 07471 80908 10058 20043 30172 40224 58004 69902 7//65 222//
       00092 333 10060 20039 3/004 55300 20000 30000
       41216 69907 88/10 91017 90760 91118 90760 91216==
# SYNOPS from 10113, Norderney (Germany) | 53-43N | 007-09E | 11 m
202212041800 AAXX 04181 10113 05574 80808 10053 20022 30194 40214 53002 60002
        333 10054 20005 3/000 55300 20000 30000 60007
        83/21 88/31 91012 90760 91114 90760 91209==
# SYNOPS from 10124, Leuchtturm Alte Weser (Germany) | 53-52N | 008-08E | 30 m
202212041800 AAXX 04181 10124 46/// /0511 10050 20030 30173 40212 53001
        333 10050 20006 55300 90760 91114==
# SYNOPS from 10131, Cuxhaven (Germany) | 53-52N | 008-42E | 5 m
202212041800 AAXX 04181 10131 05464 70607 10050 20031 30200 40215 55001 60002
       333 10050 20012 3/001 55300 20000 30000 60007
       87/13 91009 90760 91112 90760 91209==
# SYNOPS from 10147, Hamburg-Fuhlsbuettel (Germany) | 53-38N | 010-00E | 16 m
202212041800 AAXX 04181 10147 05363 80706 10042 20024 30195 40214 55000 60002
        333 10043 21002 3/000 55300 20000 30000 41188
        60007 88/09 91010 90760 91110 90760 91207==
```

FM15 METAR Surface Observation for Aviation

METAR/SPECI from EDDF, Frankfurt/Main (Germany). SA 04/12/2022 22:50-> METAR EDDF 042250Z AUTO 01004KT 9999 -RA FEW007 BKN016 02/01 Q1015 BECMG BKN013= SA 04/12/2022 22:20-> METAR EDDF 042220Z AUTO 02006KT 350V050 9000 -RADZ BKN016 BKN024 02/01 Q1015 TEMPO BKN014= SA 04/12/2022 21:50-> METAR EDDF 042150Z AUTO 03005KT 360V060 9999 -RADZ FEW006 OVC017 03/01 Q1015 NOSIG= SA 04/12/2022 21:20-> METAR EDDF 042120Z AUTO 03007KT 9999 -RA OVC019 03/01 Q1014 NOSIG= SA 04/12/2022 20:50-> METAR EDDF 042050Z AUTO 04009KT 9999 BKN020 03/01 Q1014 NOSIG= SA 04/12/2022 20:20-> METAR EDDF 042020Z AUTO 04010KT 9999 -DZ BKN021 03/01 Q1014 NOSIG= SA 04/12/2022 19:50-> METAR EDDF 041950Z AUTO 04010KT 9999 FEW009 BKN025 OVC032 03/01 Q1014= SA 04/12/2022 19:20-> METAR EDDF 041920Z AUTO 03009KT 9999 BKN020 OVC031 03/01 Q1014 NOSIG= SA 04/12/2022 18:50-> METAR EDDF 041850Z AUTO 05010KT 9999 BKN019 03/01 Q1014 NOSIG= SA 04/12/2022 18:20-> METAR EDDF 041820Z AUTO 02009KT 9999 -RA FEW016 03/01 Q1013 NOSIG= SA 04/12/2022 17:50-> METAR EDDF 041750Z AUTO 02008KT 9999 -RA SCT018 03/01 Q1013 BECMG OVC013= SA 04/12/2022 17:20-> METAR EDDF 041720Z AUTO 02008KT 9999 -RA BKN016 03/00 Q1014 BECMG OVC013= SA 04/12/2022 16:50-> METAR EDDF 041650Z AUTO 03009KT 9999 OVC015 03/00 Q1014 BECMG OVC013= SA 04/12/2022 16:20-> METAR EDDF 041620Z AUTO 03009KT 9999 OVC014 03/00 Q1014 TEMPO OVC015=

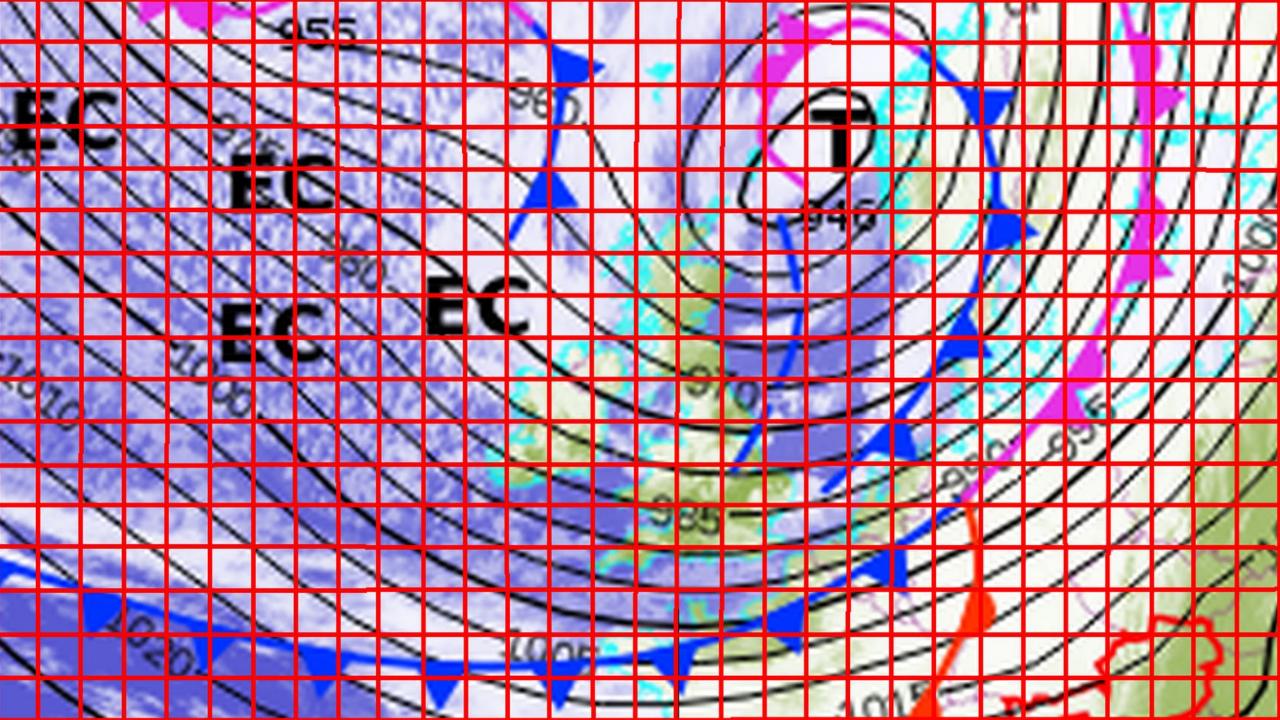
FM35 TEMP Aerological Observations (Radiosonde)



FM94 BUFR Synoptic Surface Observation

A BUFR is a binary code to encode meteorological data. The BUFR consists of sections. The following picture illustrates the different sections and their content.

		0.0	NITIN	JUOUSBI	NARVSTE	PEΔM				
CONTINUOUSBINARYSTREAM										
Section Secti		ion	Section	Section	Section	Section				
0		1	2	3	4	5				
Section	Name Contents									
Number										
0	Indicator Section "BUFR" (coded according to the CCITT International Alphabet No. 5, which is functionally equivalent to ASC length of message, BUFR edition number									
1	Identifi Section		Leng	th of section,	ction, identification of the message					
2	Optional Section and any additional items for local data processing centers					ocal use by				
3	Data Descri Sectio		Length of section, number of data subsets, data category flag, data compression flag, and a collection of data descriptors which define the form and content of individual data elements							
4	Data S	Section	Length of section and binary data							
5	End S	ection	"7777" (coded in CCITT International Alphabet No. 5)							



CODES IN METEOROLOGICAL OPERATIONS FM92 GRIB Synoptic Surface Observation

- > GRIdded Binary
- > Is a 'table-driven' Code
 - > All Metadata are include (Model, Time-Date, Parameter etc)
- > Is nor readable by man, only for computer processing (binary)
- > Requires special programs for visualization
- > Is available in the web as meteorological charts
 - www.passageweather.com
 - > www.vorticity.de

Full set, single charts

Selected sets, visualized with classic charts, <u>HINDCAST</u> verification etc

CODES IN METEOROLOGICAL OPERATIONS FM92 GRIB Synoptic Surface Observation

- > Advantages of GRIB
- > Easy selection of areas of interest (ship's position)
- > Easy integration of weather information into navigation systems (moving map)
- Disadvantages
- Just read as ,Wind at position N45 W030 : 250° 25knots
- > is binary information: right or wrong

Important is the synoptic interpretation of GRIB charts to understand what's going on in the atmosphere

North Atlantic Wind Sea MSL Pressure

Numerical Weather Prediction ...

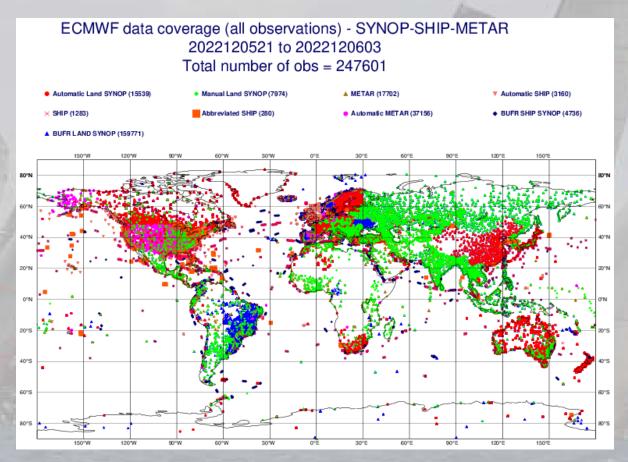
... is an initial value problem – Problems:

- 1. Initial State, i.e. Observations...
- 2. Physical Modelling
- 3. Physical (subscale) Parametrization

Solution of these Problem:

Numerical Weather Prediction ...

1. Initial State, i.e. Observations ...



Numerical Weather Prediction ...

- 1. Initial State, i.e. Observations...
- 2. Physical Modelling
- 3. Parameterization

Mathematical Describtion of sub-scale processes e.g. Shower / Thunderstorms boundary layer phenomena etc

As long as that is required – DMO post-processing is appropriate, e.g. MOS – Model Output Statistics

Post-Processing: Statistical Interpretation

Multiple linear regression equations ...

- MOS Model Output Statistics
 - ... between observations and forecasts of numerical models

- PP Perfect Prog
 - ... between observations and analyses

Post-Processing: MOS Model Output Statistics

```
Predictand Predictors...

• StF_T2m = const * DMO_T2m

- const * rH_1000_hPa

+ const
```

- Know-How is in the definition of predictors
 - > Wind components (coastlines, mountains)
 - Upper-air flow patterns (vorticity)
 - > TS-Indices, binary-predictors (model changes)

Post-Processing: MOS Model Output Statistics

MOS Pros

- Each observed parameter can be forecasted (also visibility, ceiling, even the forecast error)
- > Correction of systematic model errors
- > Consideration of local topography
- > Is quasi "Parameterization" of synoptic experience

MOS Cons

- Depends on specific NWP models
- > Model changes have to be considered

Post-Processing: Perfect Prog

- PP Pros
 - Long time-series available (Re-Analysis)
 - > Independent from NWP-model used

- PP Cons
 - > Does not correct for model errors
 - > Limited predictands (e.g. no visibility)



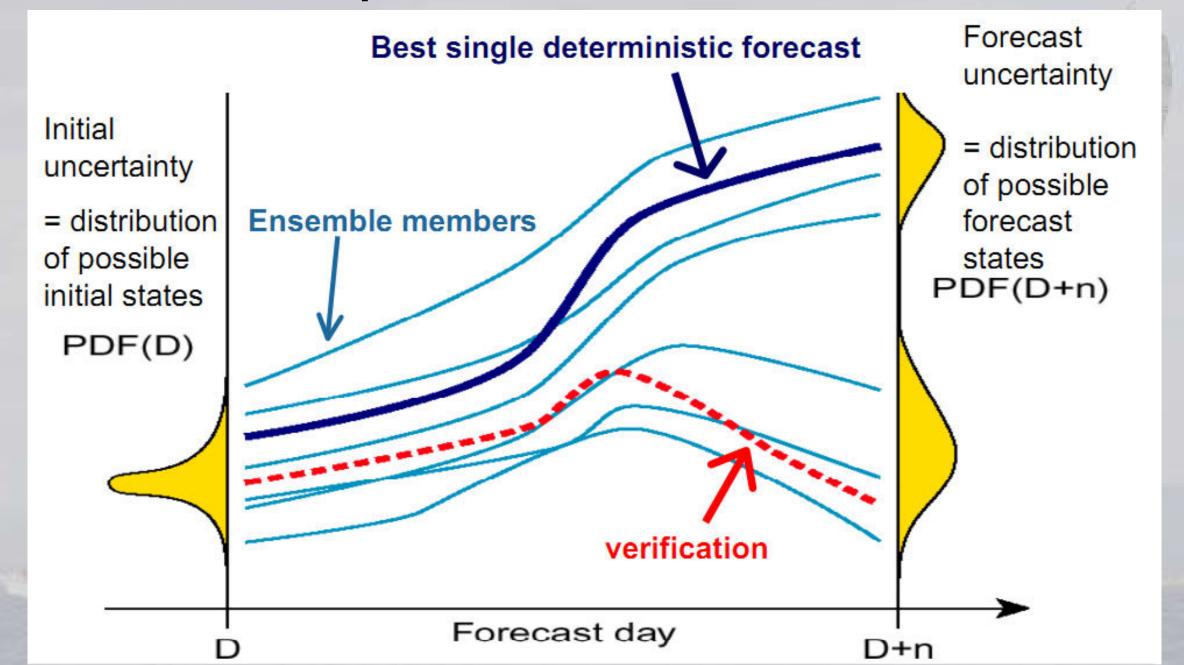
Butterfly effect

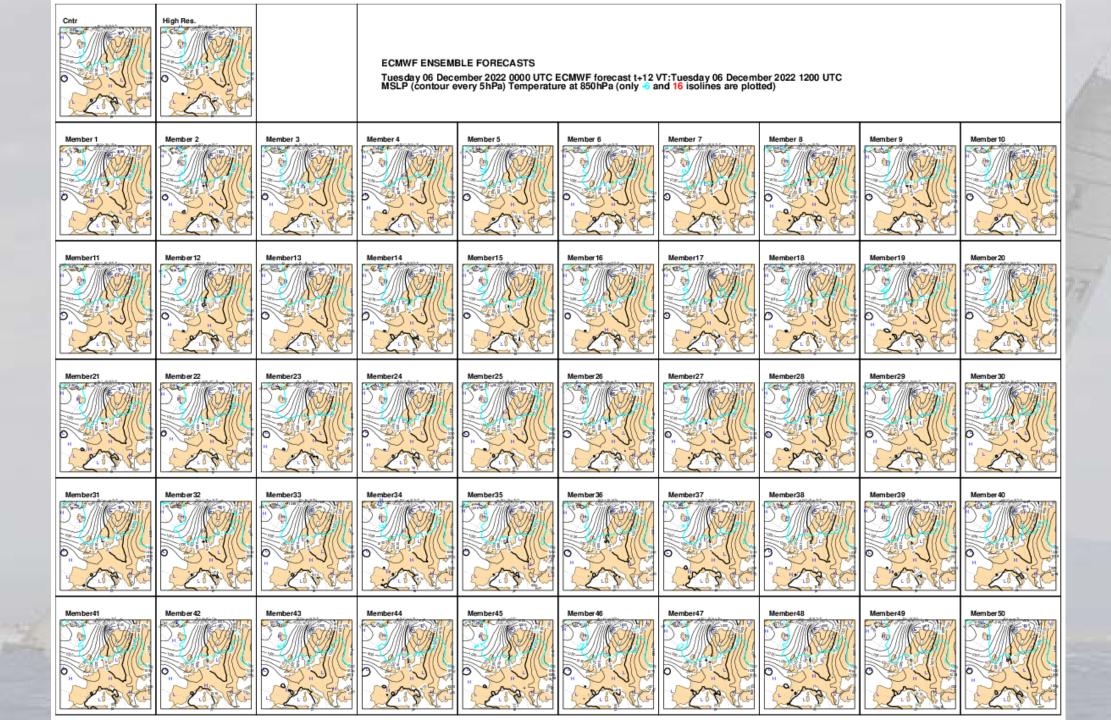
Edward Lorenz 1972

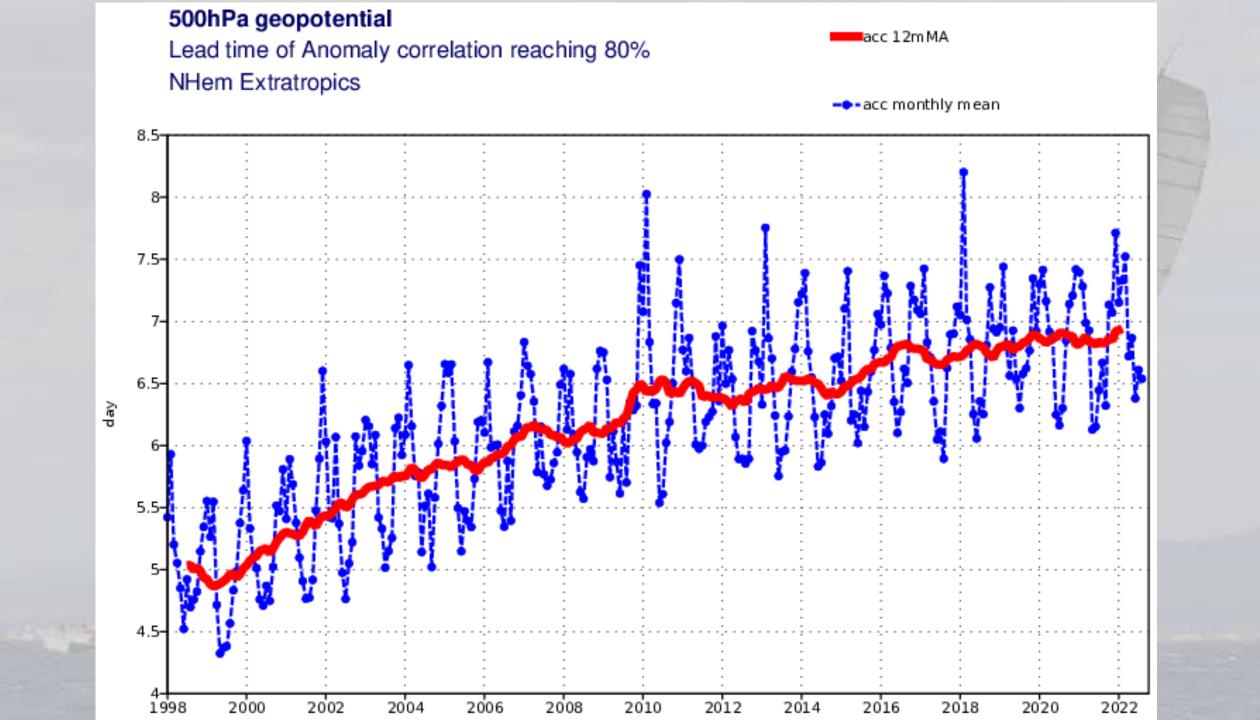
Predictability:

Does the flap of a butterfly's wings in Brazil set off a tornado in Texas?

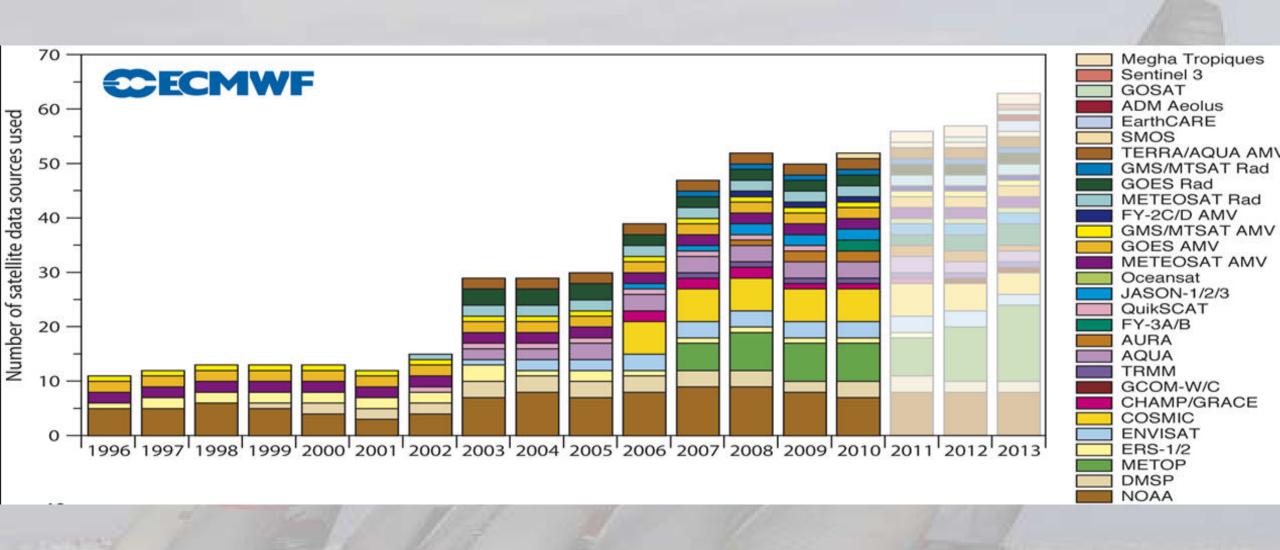
Another Forecast Optimization: Ensemble Forecast

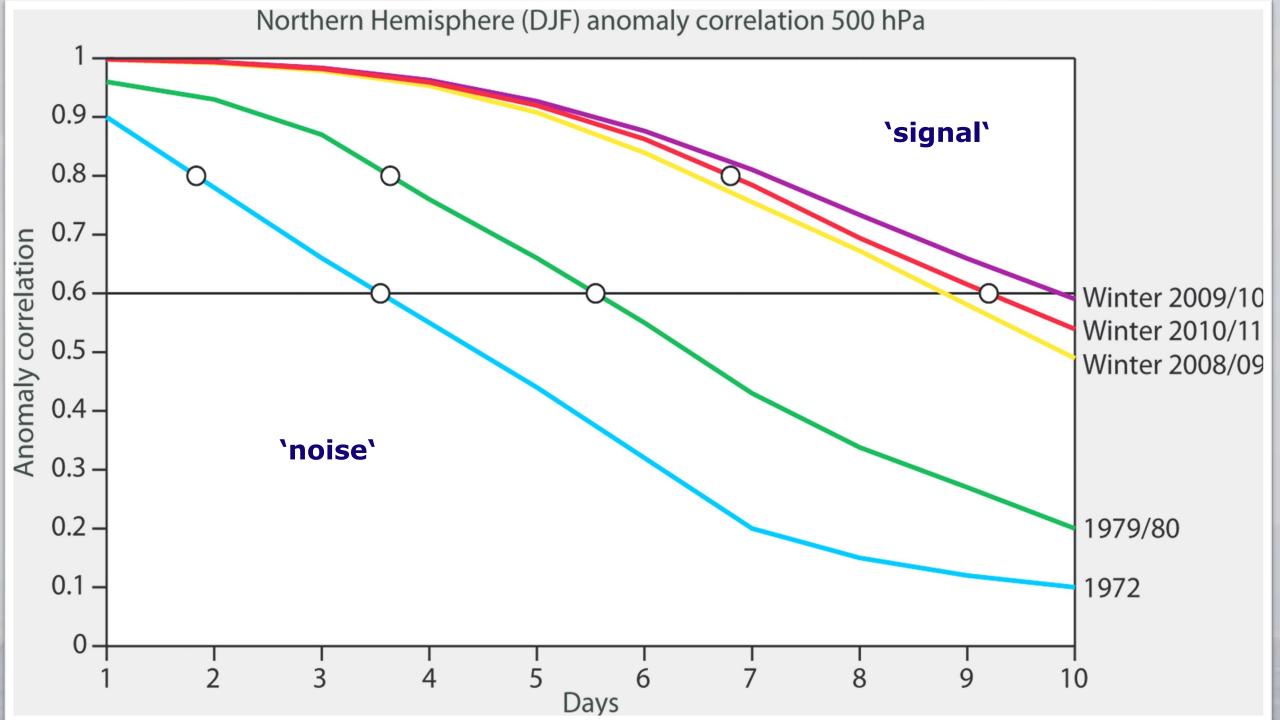




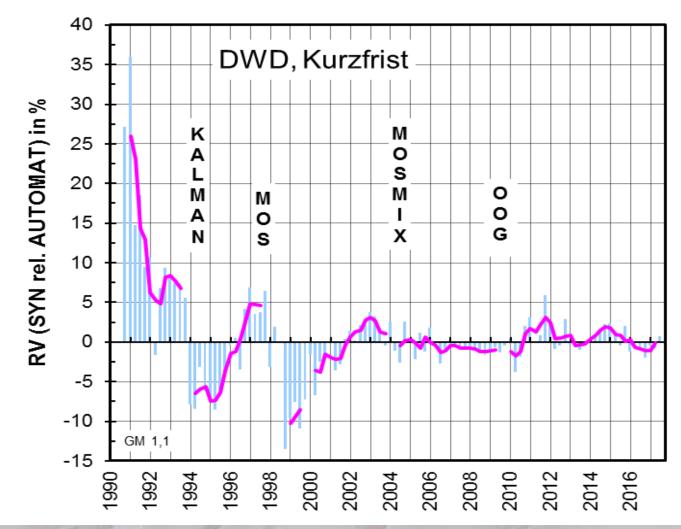








Comparison: WoMan (+NWP!) vs NWP + Post Processing



RV (Reduction of variance) describes quality improvement. Positive values: Man (+computer!) is better than computer. A method promising 15% RV reduction is worth to be used!

QUESTIONS YOU SHOULD BE ABLE TO ANSWER

Numerical Weather Prediction NWP

- ✓ How would you describe NWP?
 - ✓ NWP is an initial state problem, characterized by 6 equations (primitive equations, some of them time-dependent) for 6 variables (Pressure, Humidiy, density, 3 wind components). These equations are computed for the future: forecast!
- ✓ What are typical resolutions (grid mesh-size) for NWP model?
 - ✓ Global tens of km, Regional (fine-mesh) a few km
- ✓ Which is the problem of the limited mesh-size
 - ✓ There are (sub-grid) phenomena that cannot be resolved by the model, e.g. shower, thunderstorm, land-sea-breeze, local valley winds. These phenomena are parameterized, i.e. decribed by formulas.
- ✓ What is required for numerical stable modelruns?
 - ✓ Compliance with the Courant-Friedrich-Lewy-condition
 - ✓ Ratio between mesh-size and timestep (violated by Richardson 1921)

QUESTIONS YOU SHOULD BE ABLE TO ANSWER

Numerical Weather Prediction

- ✓ How can you improve forecasts based on the DMO (Direct Model Output)
 - ✓ By statistical post-processing. This covers adaptive filters (Kalman) and statistical processing, typical MOS (Model Output Statistics) and PP (Perfect Prog)

post-

- ✓ What is the difference between MOS and Perfect Prog?
 - ✓ Both are based on multiple linear regression equations ...
 - ✓ ... MOS between observations and DMO Model Output field (typical 5 years)
 - ✓ ... Perfect Prog between observations and Analyses only (typical 40 years)
- ✓ What are main Pros and Cons of both?
 - ✓ MS Pros: corrects systematic NWP errors,
 - ✓ MS-Pros: allows forecast of all observed parameters (not computed by the model though)
 - ✓ MS-Cons: Model-specific development, model changes have to be corrected for
 - ✓ PP-Pros: Information of 40 years is used
 - ✓ PP-Pros: Can be used for any model, not model-specific (Forecast considered Perfect, PP)
 - ✓ PP-Cons: Can be used for any model, not model-specific: does not correct model errors

QUESTIONS YOU SHOULD BE ABLE TO ANSWER

Numerical Weather Prediction

- ✓ What is the idea behind Ensemble Forecast Technology?
 - ✓ NWP models are sensitive against infinitesimal errors in the initial state, therefore 50 simplified model versions are run with infinitesimal changes of the initial state and the results are interpreted by 'clustering'

✓

Please check vorticity – ENG – MISCellaneous https://www.vorticity.de//vorticity_en.php#0_ANKER_V

QUESTIONS YOU SHOULD BE ABLE TO ANSWER **Numerical Weather Prediction** ✓ What ✓ Mo ✓ What ✓ Mo ✓ What ✓ Mo ✓ What ✓ Mo

QUESTIONS YOU SHOULD BE ABLE TO ANSWER **Numerical Weather Prediction** ✓ What ✓ Mo ✓ What ✓ Mo ✓ What ✓ Mo ✓ What ✓ Mo

QUESTIONS YOU SHOULD BE ABLE TO ANSWER **Numerical Weather Prediction** ✓ What ✓ Mo ✓ What ✓ Mo ✓ What ✓ Mo ✓ What ✓ Mo

